Crystal Structure of the 4H BaCrO₃ Polytype

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The structure of the four-layer hexagonal BaCrO₃ polytype, prepared at high temperature and high pressure, was determined utilizing a Picker FACS-I diffractometer. The hexagonal black crystal was found to crystallize with a four-layer stacking sequence in space group $P6_3/mmc$ having unit cell parameters a = 5.660(1) and c = 9.357(1) Å. The structure was determined from 668 independent reflections of which 605 were considered observed. Equivalent reflections were averaged and this operation yielded 130 unique, observed reflections. Refinement of the structure by least-squares methods gave a conventional R value of 3.0%. The structure consists of a four-layer stacking sequence of close-packed BaO₃ layers containing tetravalent chromium in all the octahedral oxygen interstices. The compound was found to be isostructural with β -BaMnO₃ and the recently reported BaRhO₃ and SrMnO₃.

Introduction

The BaCrO₃ system was reported (1) to form a variety of different BaMO₃ polytypes. The most stable and recurring forms were the 4H and 6H varieties. The structures of other BaCrO₃ polytypes have been reported, 14H (2) and 27R (3). The structure of a nonstoichiometric and nonperovskite-related Ba/Cr/O product was also determined (4).

In an effort to correlate the structure of the various $BaCrO_3$ polytypes with their magnetic and electrical properties, a study of the structure of the remaining polytype was originated.

Experimentation

Preparation. The preparation of $BaCrO_3$ was performed in a tetrahedral anvil apparatus under a variety of conditions and uti-

lizing various reactants. The synthesis of this particular polytype was through the reaction of Ba₂CrO₄ and CrO₂ at 1000°C and 60-65 kbar for 1 hr. Powder diffraction studies and preliminary single-crystal studies indicated the presence of the four-layer analog of BaCrO₃. Several single crystals, isolated in the form of black hexagonal plates, showed the characteristic pattern of a four-layer structure. Indexation of the powder pattern was successfully carried out by the close analogy of the pattern with that of the isostructural high-temperature form of BaMnO₃ (4H). The high-pressure products were washed in dilute HCl to isolate a product free from acid-soluble reactants such as BaO, BaCO₃, and Ba₂CrO₄.

Crystallographic studies. Preliminary Xray powder diffraction analysis of the product indicated a four-layer BaMO₃ polytype. Precession data taken on several single crystals showed the characteristic fourlayer repeat sequence in the hh0l and hk0l precession photographs.

The hexagonal plates from individual high-pressure experiments were studied by the precession method and were all found to possess hexagonal symmetry with a fourlayer stacking sequence. The space group was found to be $P6_3/mmc$, $P6_3 mc$, or $P\overline{6} 2c$ and the unit cell parameters from the precession data suggested a = 5.659 and c = 9.321 Å. The Guinier data on the powdered product yielded the parameters a = 5.692(3) and c = 9.3592(7) Å, where the figures in parentheses represent the standard deviations in the last reported figure.

Structure determination. The unit cell parameters for the crystal used in the singlecrystal experiment were determined in the PICK-II least-squares refinement program using 28 reflections within the angular range $31^{\circ} < 2\theta < 53^{\circ}$; the reflections were automatically centered on a Picker FACS-I four-circle diffractometer using Mo K α_1 radiation ($\lambda = 0.70930$ Å). The unit cell parameters were found to be a = 5.660(1) and c = 9.357(1) Å. The calculated volume is 259.63 Å³, giving a calculated density, with Z = 4, of 6.07 g cm⁻³.

A crystal with hexagonal bipyramid shape $(0.20 \times 0.20 \times 0.29 \text{ mm})$ (vol. = 6.45 $\times 10^{-6} \text{ cm}^3$) was used for data collection. Precise dimensions of the crystal were determined with a microscope utilizing high magnification. These data were used in an absorption correction program written by N. W. Alcock and modified by B. Lee for a crystal of general shape.

Diffraction intensities were measured using Zr-filtered Mo $K\alpha_1$ radiation at a takeoff angle of 1.5° with the diffractometer operating in the ω scan mode. Ten-second background counts were taken at both ends of a 1.4° θ -2 θ offset corrected for dispersion. Of the 668 data collected in the angular range $2\theta < 54^\circ$, 605 were considered observable according to the criterion $|F_0| > 3.0 \sigma_F$, where σ_F is defined as 0.02 $|F_0| + [C + k^2]$ $B_1^{1/2}/2 |F_0| Lp$; the total scan count is C, k is the ratio of scanning time to the total background time, and B is the total background count. Three reflections were systematically monitored as standards during the experiment; the maximum variation in intensity observed was never greater than $\pm 3\%$ over the data collection period.

Intensity data were corrected for Lorentzian and polarization effects, and absorption corrections were carried out using the computer program already cited. The corrected data were then averaged using a program written by L. Finger (5) using the hexagonal transformation for determining equivalent reflections. This generated 130 independent reflections and these were assigned positive *hkl* values prior to refinement.

Structure refinement. The study of the precession photographs indicated a fourlayer stacking sequence of BaO₃ layers with Cr located in octahedral interstices. Since this system was previously observed for (high-temperature form) BaMnO₃ (6), BaRhO₃ (7), and SrMnO₃ (8) systems, it was decided to attempt the refinement based on this particular ABO_3 structure. The most probable space group for these hexagonal polytypes is taken as $P6_3/mmc$ (No. 194).

A full-matrix refinement (9) using the positional parameter for five atoms, a $1/\sigma^2$ weighting scheme, zero-valent scattering factors for Ba, Cr, and O (10), isotropic temperature factors, and corrections for secondary extinction and anomalous dispersion yielded a residual R = 0.12 and a weighted residual $R_w = 0.22$. The final anisotropic refinement, based on a data: parameter ratio of 8.7 with the 15 independently varied parameters, yielded R = 0.030 and R_w = 0.042 for the observed data.

Table I presents the positional and anisotropic temperature parameters from the final anisotropic refinement. Except for the two ripples at the periphery of the Ba at-

| Atomic Parameters for BaCrO ₃ (4H) | | | | | | | | | | | | | |
|-----------------------------------------------|------------|---------------|--------|-----------|----------------|----------------|-------------------------|--|--|--|--|--|--|
| Atom | Position | x | у | Z | $B_{11}{}^{a}$ | $B_{22}{}^{a}$ | B_{33}^{a} 1.63(3) | | | | | | |
| Ba(1) | 2 <i>a</i> | 0 | 0 | 0 | 0.77(7) | b | | | | | | | |
| Ba(2) | 2c |] | 23 | 14 | 1.09(7) | ь | 0.18(2) | | | | | | |
| Cr | 4f | 13 | 23 | 0.6105(2) | 0.73(10) | b | 0.20(2) | | | | | | |
| O(1) | 6g | $\frac{1}{2}$ | 0 | 0 | 1.17(32) | 1.78(36) | 0.20(8) | | | | | | |
| O(2) | 6 <i>h</i> | 0.3705(13) | 0.1852 | 14 | 0.97(32) | 2.20(32) | 0.27(8) | | | | | | |

TABLE I

^a Thermal parameters are multiplied by 100. The B's are defined by the general temperature factor exp $\left[-\frac{1}{4}(B_{11}h^2a^{*2} + B_{22}k^2b^{*2} + B_{33}l^2c^{*2} + 2B_{12}hka^*b^* + 2B_{13}hla^*c^* + 2B_{23}klb^*c^*)\right].$

^b For Ba and Cr atoms, B_{22} and B_{12} were not refined since $B_{11} = B_{22}$, and $B_{12} = \frac{1}{2}B_{11}$. For O(2), the y parameter was not refined since $y = \frac{1}{2}x$; and $B_{12} = \frac{1}{2}B_{22}$.

oms, the difference Fourier map was essentially flat and equivalent to 0.2 of an oxygen atom or less.

An illustration of the structure is given in Fig. 1. The figure was prepared using OR-TEP (11). Bond lengths and angles calculated in the ORFFE program are given in Table II. The table of observed and calculated structure factors comprises Table III.

Results and Discussion

Of the first-row transition metals, $BaMnO_3$ was first observed (6) to form a variety of different BaMO₃ polytypes based on the perovskite structure. The relationship between the cubic perovskite structure and hexagonal layer structures was established by Katz and Ward (12) in 1964.

The four-layer stacking sequence ABAC, or the packing sequence $(hc)_2$, has the Zhdanov notation |(1)(1)|. The structure consists of pairs of face-shared octahedra which are further linked by vertices along the c axis of the unit cell. The polyhedral representation of the structure is shown in Fig. 1. This structural type has been reported for β -BaMnO₃, SrMnO₃, the highpressure forms of BaRuO₃ (13) and BaRhO₃ (7), and the solid solutions of $BaRuO_3/Sr$ -RuO₃ and BaMnO₃/SrMnO₃. Lattice images of 4H BaCrO₃ were studied by Gai et al. (14) and their results were interpreted as showing the $(ch)_2$ stacking sequence.

This stable structure represents a midpoint between the perovskite structure $(100\% \text{ cubic packing of } AO_3 \text{ layers})$ and the BaNiO₃ structure (100% hexagonal packing of AO_3 layers). The consequence of the alternating of cubic and hexagonal packing leads to face-shared octahedral units which allow a short metal-to-metal distance for the transition metal ions. For the four-layer



FIG. 1. The projection of the hexagonal (110) plane for BaCrO₃ (4H).

B. L. CHAMBERLAND

| | | Dista (Å | inces A) | | | Angles (°) | | | | | |
|--------------------------------------------|----------|----------------------------------------------|-----------------------------|----------------|------------------------------------|------------------------------------------------|----------------------|--------------------------------------------------|--|--|--|
| Ba(1)-O(1) -O(2) | 6@ 6@ | 2.830(1) 2.962(4) | O(1)-O(1) -O(2) | 4@ 4@ | 2.830(1) 2.807(2) | O(1)-Cr-O(1) -O(2) -O(2) O(2)-Cr-O(2) | 3@ 3@ 6@ 3@ | 94.08(7) 170.35(17) 92.49(10) 80.16(20) | | | |
| Ba(2) -O(1) -O(2) | 6@ 6@ | 2.836(4) 2.854(1) | O(2)-O(2) -O(1) -O(2) | 2@ 4@ 2@ | 2.514(11) 2.807(2) 3.146(11) | | | | | | |
| Cr -O(1) -O(2) Cr -Cr Cr-O (1)-Cr | 3@ 3@ | 1.934(1) 1.952(5) 2.611(4) 3.867(2) | | | | Cr-O(2)-Cr Cr-O(1)-Cr | | 83.94(27) 180.0 | | | |

TABLE II Bond Lengths and Angles in BaCrO₃ (4H)

TABLE III Observed and Calculated Structure Factors (5x)

| h | k | l | Fobs | FCALC | h | k | 1 | F _{obs} | FCALC | h | k l | F _{OBS} | FCALC | h | k | 1 | F _{obs} | FCALC | h | k l | F _{OBS} | FCALO |
|---|---|----|------|-------|---|----|----|------------------|-------|---|-----|------------------|-------|---|---|----|------------------|-------|---|-----|------------------|-------|
| 0 | 0 | 2 | 50 | 51 | 0 | 3 | 10 | 47 | 41 | 1 | 3 (| 19 | 16 | 2 | 0 | 1 | 295 | 289 | 2 | 4 2 | 363 | 354 |
| 0 | 0 | 4 | 755 | 736 | 0 | 5 | 0 | 54 | 62 | 1 | 3 1 | 106 | 106 | 2 | 0 | 2 | 791 | 764 | 2 | 43 | 312 | 310 |
| 0 | 0 | 6 | 263 | 280 | 0 | 5 | 1 | 97 | 98 | 1 | 3 2 | 381 | 392 | 2 | 0 | 3 | 686 | 673 | 2 | 44 | 174 | 166 |
| 0 | 0 | 8 | 699 | 699 | 0 | 5 | 2 | 256 | 260 | 1 | 3 3 | 392 | 397 | 2 | 0 | 4 | 308 | 304 | 2 | 45 | 224 | 219 |
| 0 | 0 | 10 | 43 | 48 | 0 | 5 | 3 | 296 | 306 | 1 | 34 | 171 | 165 | 2 | 0 | 5 | 437 | 439 | 2 | 46 | 302 | 283 |
| 0 | 1 | 0 | 37 | 33 | 0 | 5 | 4 | 165 | 163 | 1 | 3 5 | 260 | 263 | 2 | 0 | 6 | 535 | 521 | 2 | 50 | 461 | 455 |
| 0 | 1 | 1 | 117 | 111 | 0 | 5 | 5 | 208 | 214 | 1 | 3 6 | 303 | 303 | 2 | 0 | 7 | 121 | 121 | 2 | 51 | 30 | 25 |
| 0 | 1 | 2 | 593 | 567 | 0 | 5 | 6 | 213 | 204 | 1 | 37 | 44 | 43 | 2 | 0 | 8 | 65 | 62 | 3 | 30 | 565 | 593 |
| 0 | 1 | 3 | 605 | 595 | 0 | •5 | 7 | 41 | 37 | 1 | 38 | 95 | 90 | 2 | 0 | 9 | 253 | 252 | 3 | 32 | 20 | 26 |
| 0 | 1 | 4 | 242 | 230 | 1 | 1 | 0 | 1128 | 1157 | 1 | 39 | 167 | 162 | 2 | 0 | 10 | 154 | 168 | 3 | 34 | 207 | 213 |
| 0 | 1 | 5 | 354 | 356 | 1 | 1 | 2 | 46 | 41 | 1 | 4 (| 633 | 664 | 2 | 0 | 11 | 326 | 315 | 3 | 36 | 136 | 141 |
| 0 | 1 | 6 | 397 | 398 | 1 | 1 | 4 | 324 | 306 | 1 | 4 1 | 23 | 23 | 2 | 2 | 0 | 998 | 1046 | 3 | 40 | 49 | 50 |
| 0 | 1 | 7 | 37 | 39 | 1 | 1 | 6 | 245 | 256 | 1 | 4 2 | 33 | 30 | 2 | 2 | 2 | 54 | 51 | 3 | 4 1 | 80 | 77 |
| 0 | 1 | 8 | 119 | 126 | 1 | 1 | 8 | 477 | 475 | 1 | 4 3 | 22 | 23 | 2 | 2 | 4 | 439 | 437 | 3 | 42 | 216 | 215 |
| 0 | 1 | 9 | 202 | 203 | 1 | 1 | 10 | 61 | 49 | 1 | 4 4 | 232 | 228 | 2 | 2 | 6 | 175 | 182 | 4 | 00 | 72 | 86 |
| 0 | 1 | 10 | 73 | 87 | 1 | 2 | 0 | 49 | 48 | 1 | 4 5 | 20 | 18 | 2 | 2 | 8 | 515 | 505 | 4 | 01 | 165 | 166 |
| 0 | 1 | 11 | 292 | 286 | 1 | 2 | 1 | 129 | 134 | 1 | 4 6 | 152 | 158 | 2 | 3 | 1 | 77 | 75 | 4 | 02 | 461 | 478 |
| 0 | 3 | 0 | 832 | 902 | 1 | 2 | 2 | 411 | 408 | 1 | 47 | 27 | 18 | 2 | 3 | 2 | 345 | 356 | 4 | 03 | 413 | 425 |
| 0 | 3 | 1 | 43 | 46 | 1 | 2 | 3 | 488 | 491 | 1 | 48 | 332 | 332 | 2 | 3 | 3 | 314 | 322 | 4 | 04 | 211 | 211 |
| 0 | 3 | 2 | 42 | 39 | 1 | 2 | 4 | 232 | 227 | 1 | 5 0 | 35 | 41 | 2 | 3 | 4 | 134 | 127 | 4 | 05 | 287 | 296 |
| 0 | 3 | 3 | 33 | 43 | 1 | 2 | 5 | 316 | 320 | 1 | 5 1 | 91 | 87 | 2 | 3 | 5 | 215 | 212 | 4 | 06 | 366 | 368 |
| 0 | 3 | 4 | 266 | 269 | 1 | 2 | 6 | 326 | 314 | 1 | 52 | 262 | 260 | 2 | 3 | 6 | 284 | 278 | 4 | 07 | 83 | 81 |
| 0 | 3 | 5 | 34 | 31 | 1 | 2 | 7 | 56 | 53 | 1 | 53 | 279 | 273 | 2 | 3 | 7 | 27 | 26 | 4 | 08 | 42 | 44 |
| 0 | 3 | 6 | 191 | 211 | 1 | 2 | 8 | 88 | 85 | 1 | 54 | 130 | 132 | 2 | 3 | 8 | 93 | 92 | 4 | 09 | 193 | 188 |
| 0 | 3 | 7 | 38 | 28 | 1 | 2 | 9 | 193 | 193 | 1 | 55 | 190 | 190 | 2 | 4 | 0 | 73 | 72 | 6 | 00 | 569 | 562 |
| 0 | 3 | 8 | 412 | 412 | 1 | 2 | 10 | 59 | 62 | 2 | 0 0 | 116 | 119 | 2 | 4 | 1 | 116 | 114 | 6 | 02 | 50 | 50 |

 $BaMO_3$ analogs these distances are 2.61 Å in BaCrO₃, 2.63 Å in BaMnO₃, and 2.63 Å in BaRhO₃. These short distances result from some d orbital overlap between neighboring metal atoms. The Cr-Cr distance observed in other BaCrO₃ polytypes varies slightly (average distances are given): 4H (2.61 Å), 6H (2.65 Å), 14H (2.64 Å), and 27R (2.63 Å). The observed metal-to-metal distance in the 4H polytype of BaCrO₃ was found to be the shortest and this particular polytype possesses the largest amount of hexagonal packing character. A strong correlation between these two factors was developed from these structural investigations.

All the other features of the structure for the four-layer polytype of $BaCrO_3$ are consistent with the model. The average Cr-Obond distance of 1.94 Å is in agreement with the predicted (15) value of 1.95 Å. The twelve-coordinated sites for each Ba atom are well behaved and no unusual features were encountered in the structural determination.

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